Full particle-in-cell simulation of the interaction between two plasmas for laboratory experiments on the generation of magnetized collisionless shocks
with high-power lasers

Takayuki Umeda,1, a) Ryo Yamazaki,2, b) Yutaka Ohira,3, c) Natsuki Ishizaka,2 Shin Kakuchi,2 Yasuhiro Kuramitsu,4 Shuichi Matsukiyo,5 Itaru Miyata,2 Taichi Morita,5 Youichi Sakawa,6 Takayoshi Sano,6 Shuto Sei,2 Shuta J. Tanaka,2 Hirohumi Toda,2 and Sara Tomita2
1) Institute for Space-Earth Environmental Research, Nagoya University, Nagoya 464-8601, JAPAN
2) Department of Physics and Mathematics, Aoyama Gakuin University, Sagamihara 252-5258, JAPAN
3) Department of Earth and Planetary Science, The University of Tokyo, Tokyo 113-0033, JAPAN
4) Graduate School of Engineering, Osaka University, Osaka 565-0871, JAPAN
5) Faculty of Engineering Sciences, Kyushu University, Kasuga 816-8580, JAPAN
6) Institute of Laser Engineering, Osaka University, Osaka 565-0871, JAPAN

A preliminary numerical experiment is conducted for laboratory experiments on the generation of magnetized collisionless shocks with high-power lasers by using one-dimensional particle-in-cell simulation. The present study deals with the interaction between a moving Aluminum plasma and a Nitrogen plasma at rest. In the numerical experiment, the Nitrogen plasma is unmagnetized or magnetized by a weak external magnetic field. Since the previous study suggested the generation of spontaneous magnetic field in the piston (Aluminum) plasma due to the Biermann battery, the effect of the magnetic field is of interest. Sharp jumps of electron density and magnetic field are observed around the interface between the two plasmas as long as one of the two plasmas is magnetized, which indicates the formation of tangential electron-magneto-hydro-dynamic discontinuity. When the Aluminum plasma is magnetized, strong compression of both density and magnetic field takes place in the pure Aluminum plasma during the gyration of Nitrogen ions in the Aluminum plasma region. The formation of a shock downstream is indicated from the shock jump condition. The result suggests that the spontaneous magnetic field in the piston (Aluminum) plasma plays an essential role in the formation of a perpendicular collisionless shock.

I. INTRODUCTION

Collisionless shocks play important roles in the generation of high-energy particles in various situations, which is one of the most important outstanding issues in plasma physics.1,2 Recently, laboratory experiments using high-power lasers are conducted on the generation of collisionless shocks propagating into unmagnetized3–6 and magnetized7–11 plasmas. In particular, the laboratory experiments of magnetized collisionless shocks are of great interest since the most astrophysical and solar-terrestrial plasmas hosting the collisionless shocks are magnetized.

There are mainly two ways to excite collisionless shocks in laboratory plasma experiments using high-energy lasers, in which two plasmas collide with each other. One is to have counter-streaming plasmas, both of which move in the laboratory frame. They arise from double-plane targets irradiated by lasers.9,10 In the other way,11 an ambient plasma at rest is pushed by a flowing plasma originated in laser ablation. To make the ambient plasma, the neutral gas is fulfilled around the target before the shot, and it is photoionized by photons generated in the laser ablation process. The ambient plasma is magnetized if the external magnetic field is imposed before it is ionized. In this method, one can easily control the field strength, accordingly the Alfvén Mach number and the plasma beta (i.e., the ratio of the plasma pressure to the magnetic pressure) of the ambient plasma. In contrast, some authors have proposed a complementary way toward the collisionless shock formation using ultra-high-intensity lasers to drive a fast quasi-neutral flow in a denser plasma.12–14

It has been believed that in the ablation plasma, spontaneous magnetic fields are produced by laser-plasma interactions due to the so-called Biermann battery process.15 The Biermann battery works when the cross product between the gradients of the electron density and the electron temperature is non-vanishing near the targets.18–20 The resultant magnetic field is toroidal with respect to the direction of the plasma flow. Then, the magnetic field convects with the ablation plasma outwards.20,21 At least just after the shot at which strong density and temperature gradients exist, the magnetic pressure can be comparable to or even larger than the kinetic and thermal pressure of the plasma. However, at present, the role of the Biermann magnetic field in the excitation of the collisionless shocks is poorly understood.

In the present study, we perform one-dimensional (1D)
full particle-in-cell (PIC) simulations of the interaction between the ablation (piston) plasma and the ambient plasma at rest, as a preliminary numerical experiment for laboratory experiment on the generation of magnetized collisionless shocks with high-power lasers such as Gekko-XII at the Institute of laser engineering in Osaka University. Since the number of shots is limited in laboratory experiments, our preliminary numerical experiments play an important role in the prediction of results of laboratory experiments. The present study aims to study the effect of the spontaneous magnetic field in the piston plasma due to the Biermann battery on the generation of collisionless shocks.

II. 1D PIC SIMULATION

A. Typical Parameters

First, we briefly describe our setup and accompanying typical parameters optimized for laboratory experiments using Gekko-XII HIPER lasers. Details will be published elsewhere. The planar Aluminum target is irradiated by HIPER lasers with energy of $\sim$ 1 kJ in total and the pulse width of $\sim$ nsec, producing the Aluminum plasma with bulk velocity of $\sim$ 10$^2$ km/s. A vacuum chamber is filled with Nitrogen gas with 5 Torr before the shot, and it is ionized by photons arising in the laser-target interaction. Just after the shot, the Aluminum plasma is very hot and dense with electron density $N_e \sim 10^{21}$ cm$^{-3}$ and temperature $T_e \sim 10^3$ eV near the target. As it expands, it adiabatically cools down and has typically $N_e \sim 10^{19}$ cm$^{-3}$ and $T_e \sim 10$ eV when the shock is formed. The Nitrogen plasma is cold with temperature $T_e \sim 1$ eV at the beginning. However, it is preheated by HIPER lasers to about several tens of eV since we consider interaction between Aluminum and Nitrogen plasmas in the ablation side of the target.

Unfortunately, the strength of the Biermann spontaneous magnetic field associated with the Aluminum plasma is unknown since magnetic fields were not measured in our preliminary laboratory experiments. Here, we roughly estimate the strength of the spontaneous magnetic field as follows. The evolution of the magnetic field is described by the following equation in SI units (so that the Boltzmann constant is omitted)

$$\frac{\partial B}{\partial t} \approx \frac{1}{eN_e} \left( \nabla T_e \times \nabla N_e \right),$$

which is derived from the rotation of the electron pressure gradient term of electric fields, i.e., $-\nabla \times \left( \nabla P_e/(eN_e) \right)$ in the magnetic induction equation. Here, we have neglected the convection term, $\nabla \times \left( U_e \times B \right)$, at the very beginning of the field generation. If we approximate $\partial/\partial t \approx V_d/\phi$ and $\nabla \approx 1/\phi$, where $V_d$ and $\phi$ are the drift velocity of the piston Aluminum plasma and the focal spot size of HIPER lasers, respectively, then we have

$$B \approx \frac{T_e}{eV_d \phi} \approx 10^3 \frac{T_e}{10^3 \text{eV}} \left( \frac{V_d}{10^2 \text{km/s}} \right)^{-1} \left( \frac{\phi}{1 \text{mm}} \right)^{-1}$$

Inserting physical parameters near the target into Eq.(2), we obtain a typical magnitude of the Biermann spontaneous magnetic field as $\sim 10$ T, which is consistent with other laboratory experiment$^{16}$ and numerical experiment.$^{17}$

On the other hand, the external magnetic field imposed on the ambient Nitrogen plasma has arbitrary strength. However, its typical value is $B \sim 1$ T. If $B \ll 1$ T, then the ion is not magnetized. If $B \gg 1$ T, then the magnetized shock propagating into the Nitrogen plasma has a small Alfvén Mach number. In the present study, we assume an unmagnetized ambient Nitrogen plasma as shown in Table.1.

B. Simulation Setup

We use a 1D relativistic full PIC code developed by ourselves that was used for simulations of collisionless shocks.$^{22}$ The Sokolov interpolation$^{23}$ is implemented into the second-order charge conservation scheme$^{24}$ to reduce numerical noises. The code has stable open boundary conditions which allows us to perform simulations with a long time of $t \gg 10^5/\omega_{pe}$. In the present numerical experiment, the simulation domain is taken along the $x$ axis. At the initial state, the simulation domain is filled with collisionless Nitrogen plasma at rest as an ambient plasma. The open boundary conditions are imposed at both of boundaries, where electromagnetic waves and plasma particles escape freely. In addition to the open boundary condition, collisionless Aluminum plasma as a piston plasma with a drift velocity $V_d$ is continuously injected from at the left boundary ($x = 0$) into the Nitrogen plasma when the numerical experiment is started. All of the plasma particles have a (shifted) Maxwellian velocity distribution with an isotropic temperature at the initial state.

The typical parameters of the Aluminum plasma and the Nitrogen plasma near a measurement point of our preliminary laboratory experiments ($\sim$ cm away from the target) are listed in Table 1. In the present numerical experiment, we have tried to use these parameters as many as possible, including the real ion-to-electron mass ratios. However, some of them are reduced with respect to the real ones to save computational cost. As an example, the vacuum permittivity $\varepsilon_0$ used in the present numerical experiment is 100 times larger than the real one. This means that the speed of light and the plasma frequency are reduced to one-tenth of the real ones. However, the Alfvén velocity, plasma beta and the inertial length are set to be the same as real ones, which are important
parameters for discussion of the shock dynamics. In Table 1, the real values in the laboratory experiments are shown at the left-hand side and reduced values are shown at the right-hand side when the physical quantity in the numerical experiment is reduced. These parameters are renormalized to the electron plasma frequency and the electron thermal velocity in the Nitrogen plasma in the full PIC simulation. The number of particles per cell for each species is also shown in Table 1.

The ambient magnetic field $B_0$ (in the Nitrogen plasma) is imposed in the $y$ direction with a magnitude of 0.5 T, in contrast to the previous studies in which the magnitude of the ambient magnetic field was 4 T. Since the magnitude of the ambient magnetic field is weak, the ambient (Nitrogen) plasma is in the high beta regime in the present study. As a spontaneous magnetic field due to the Biermann battery, we assume that the magnetic field in the piston (Aluminum) plasma is directed in the $y$ direction with a magnitude of 10 T. To magnetize the Aluminum plasma, a motional electric field is also imposed in the $z$ direction with a magnitude of $E_z = -V_d B_0$ at the left boundary ($x = 0$).

We perform four different runs. In Run 1, both of the Aluminum plasma and the Nitrogen plasma are magnetized. In Run 2, the Aluminum plasma is magnetized while the Nitrogen plasma is unmagnetized. Note that it is easy to change the magnitude of the ambient magnetic field (in the Nitrogen plasma) in laboratory experiments. In Run 3, the Nitrogen plasma is magnetized while the magnetic field in the Aluminum plasma is set to be zero to see the effect of the spontaneous magnetic field in the piston plasma. In Run 4, both of the Aluminum plasma and the Nitrogen plasma are unmagnetized. The direct comparison among these runs could show the influence of the spontaneous magnetic field in the Aluminum plasma due to the Biermann battery to the generation of collisionless shocks.

III. SIMULATION RESULT

Figure 1 shows the temporal development of the interaction between the Aluminum plasma and the Nitrogen plasma for Run 1. The ion charge density in the $x - v_x$ phase space is plotted at different times. The corresponding spatial profile of the electron density is also superimposed. Since the absolute value of the electron charge density is almost equal to the total ion charge density, i.e., the sum of charge densities of Aluminum and Nitrogen ions, the quasi charge neutrality is almost satisfied at all the time.

At the leading edge of the Aluminum plasma, there exists strong charge separation because the Aluminum ions can penetrate the Nitrogen plasma region while electrons cannot compensate the Aluminum ion charge owing to the small gyro radius. A diamagnetic current is also generated around the interface between the two plasmas due to a large magnetic shear. The charge separation and electric current excite electromagnetic fluctuations, which results in the ponderomotive force to scatter (accelerate) Aluminum ions at the leading edge toward the Nitrogen plasma region. The ponderomotive force also reflect some of Aluminum ions around the interface toward the Aluminum plasma region. Note that the acceleration of electrons due to the ponderomotive force is not seen since accelerated electrons soon diffuse in the velocity space through gyration.

As the Aluminum plasma penetrates into the Nitrogen plasma region, an instability is generated at the leading edge of the Aluminum plasma (see second and third panels at $t = 4.004$ and $8.008$ usec, respectively). We found a wave mode is excited at the local electron cyclotron frequency $\omega_{ce,local}$ from the Fourier analysis. The wavenumber satisfies the resonance condition $k_z V_{dAl} \approx \omega_{ce,local}$, suggesting that the electron cyclotron drift instability is generated due to the drift of Aluminum ions across the ambient magnetic field. For more detail, see Appendix A.

As the time elapses, the Nitrogen ions feel the motional electric field in the Aluminum plasma region and gyrate in the $x - v_x$ phase space. During the gyration, strong compression of Aluminum ions takes place in a region outside the gyration Nitrogen ions ($t = 0.35$ cm at $t = 12.012$ ns).

Panel (a) of Fig.2 shows an expansion of the ion $x - v_x$ phase space together with the spatial profile of the electron density around the interface between the two plasmas at $t = 4.004$ usec for Run 1. Panels (b) and (c) show the corresponding electron $x - v_x$ phase space together with the spatial profile of the electron temperature of the Aluminum (piston) and the Nitrogen (background) plasmas, respectively. Panel (d) shows the spatial profiles of the pressures of the piston electrons $P_{ep}$, the background electrons $P_{eb}$, the Aluminum ions $P_{AI}$, and the magnetic pressure $P_B = |B_y|^2/(2 \mu_0)$ normalized to the initial electron pressure of the Nitrogen (background) plasma region. Note that the plasma pressure is given as $P = (P_{ep} + P_{eb})/2$. The pressure of the Nitrogen ions is small and is not shown here. The magnetic field $B_y$ component is almost proportional to the total (the sum of piston and background) electron density and is not shown here.

There are two discontinuous structures (labeled as “I” and “II”) around the interface between the two plasmas. We found that the piston electrons are clearly separated from the background electrons around the discontinuity “I” as seen in panels (b) and (c) of Fig.2. The electron density, the electron temperature, and the electron pressure continuously increase from the right to the interface between the two plasmas. The density of piston electrons increases from the right to the left but the temperature of piston electrons decreases at the discontinuity “I”. The pressure of piston electrons decreases slightly (see $P_{ep}$ in Panel (d)) but the magnetic pressure increases at the discontinuity “I”. It is suggested that the electron pressure gradient force balances the $J_e \times B$ force. Since the
bulk velocities of piston and background electrons are almost the same across the discontinuity “I”, the discontinuity “II” can be regarded as a tangential electron-magneto-hydro-dynamic (EMHD) discontinuity.

Panel (c) of Fig.2 shows that the background electrons are heated due to the penetration of the piston (Aluminum) ions. The mechanism of the electron heating is considered to be the following EMHD process, since the timescale of the diffusion of electrons in the velocity space due to the gyration is fast. The background electrons feel the motional electric field of piston ions, which result in a finite bulk velocity of the background electrons \( U_{xeb} \). Then, the pressure of the background electrons increases from the right to the left, as seen in panel (d), by the compression of the background electrons, i.e., \( \partial U_{xeb}/\partial x \neq 0 \). The sum of magnetic pressure and the thermal pressure of electrons (i.e., \( P_B + 2P_eyo \)) is kept almost constant across the discontinuity “I”. Since the electron density of the piston plasma is higher than that of the background plasma, there exists a discontinuity of the electron temperature around the interface between the two plasmas.

At the discontinuity “II”, the total electron density decreases from the right to the left but the pressure of Aluminum ions increases. The sum of the pressure of Aluminum ions and the magnetic pressure is kept almost constant across the discontinuity “II”.

Panels (a) and (b) of Fig.3 show an expansion of the ion \( x - v_x \) phase space together with the spatial profile of the ion temperature of the Aluminum and Nitrogen plasmas, respectively, around the gyrating Nitrogen ions at \( t = 12.012 \) nsec for Run 1. Panel (c) shows the corresponding electron \( x - v_x \) phase space together with the spatial profile of the electron temperature. Panel (d) shows the spatial profiles of the electron bulk velocity \( U_{xe} \) and the magnetic field \( B_y \). Note that electrons in this region consist of piston electrons.

There are two discontinuous structures (labeled as “III” and “IV”) around the gyrating Nitrogen ions. At the discontinuity “III”, the electron density, the electron temperature, and the magnetic field increase from the right to the left. The electron bulk velocity changes from \( \approx 400 \) km/s to \( \approx 450 \) km/s. At the discontinuity “IV”, the electron density, the electron temperature, and the magnetic field decrease from the right to the left. The electron bulk velocity changes from \( \approx 450 \) km/s to \( \approx 500 \) km/s. The density and the magnetic field between the discontinuities “III” and “IV” are \( \approx 2.4 \) times as large as those in the unperturbed Aluminum plasma.

Let us consider the MHD shock jump conditions for perpendicular shocks,

\[
B_{y1}U_1 = B_{y2}U_2, \quad N_1U_1 = N_2U_2, \quad (m_e + m_i)N_1U_e^2 + P_1 + \frac{B^2_{y1}}{2\mu_0} = (m_e + m_i)N_2U_e^2 + P_2 + \frac{B^2_{y2}}{2\mu_0},
\]

where, the subscript “1” and “2” denotes the upstream and the downstream of a discontinuity, respectively. Here, the ion and electron densities are assumed to be almost equal, \( N \equiv N_i \approx N_e \), and the pressure is given as the sum of ion and electron pressures, \( P \equiv P_i + P_e \). The bulk velocity \( U \) is defined in rest frame of a discontinuity.

Suppose that the velocity of the discontinuities “III” and “IV” is \( \approx 485.7 \) km/s and \( \approx 414.3 \) km/s, respectively. Then, Eqs.(3) and (4) are satisfied across the discontinuities “III” and “IV” with the upstream bulk velocity of \( U_1 \approx 85.7 \) km/s, the downstream bulk velocity of \( U_2 \approx 35.7 \) km/s and the density \( N_2/N_1 \approx 2.4 \) in the rest frame of the discontinuities. From the initial conditions, we obtain \( (m_e + m_i)N_1U_e^2/P_1 \approx 206, P_{1d}/P_{1i} = 9 \) and \( B^2_{y1}/(2\mu_0P_{1i}) \approx 5.6 \). The pressures of the electrons and Aluminum ions in the high density region (downstream) are \( P_{2d}/P_{2i} \approx 11 \) and \( P_{Al2}/P_{Al1} \approx 8 \) times as large as those of the unperturbed Aluminum plasma (upstream), respectively. Then, we obtain \( (m_e + m_i)N_2U_e^2/P_2 \approx 85.8, P_{2d}/P_{2i} \approx 92 \) and \( B^2_{y2}/(2\mu_0P_{2i}) \approx 32 \). The momentum conservation law and the energy conservation law for the Aluminum plasma in Eqs.(5) and (6), respectively, are almost satisfied. Hence, the shock jump conditions are almost satisfied across the discontinuities “III” and “IV”.

This result suggests that these discontinuous structures correspond to collisionless perpendicular shocks. The high-density region between the discontinuities “III” and “IV” corresponds to the shock downstream. The typical Alfvén Mach number of the shock is \( M_A \approx 4.2 \). The shock downstream is located at a distance of one ion gyro radius of Nitrogen ions in the Aluminum plasma from the interface between the Nitrogen and Aluminum plasmas. The shock is formed on the timescale of a quarter ion gyro period of Nitrogen ions in the Aluminum plasma.

Figure 4 shows a snapshot of four Runs at \( t = 14.040 \) nsec. Panel (a) shows the \( x - v_x \) phase-space plots of electrons. Panel (b) shows the \( x - v_x \) phase-space plots of ions. Panel (c) shows the spatial profile of the magnetic field \( B_y \) component. Panel (d) shows the spatial profile of the electron density \( N_e \). Panel (e) shows the spatial profile of the electron temperature \( T_e \).

In Run 2 where the ambient magnetic field in the Nitrogen plasma is absent, the electron cyclotron drift instability is not generated at the leading edge of the Aluminum plasma. However, electron heating takes place due to the penetration of the Aluminum ions (for \( x > 0.620 \) cm), suggesting that the generation of the instability is not a necessary condition for the electron heating. The electron temperature at the leading edge of the Aluminum plasma in Run 2 is higher than that in Run 1, since elec-
trons in this region is unmagnetized and they escape from the interface. The tangential discontinuity and the shock downstream are formed at $x \approx 0.55$ cm and $x \approx 0.41 - 0.45$ cm, respectively. The comparison between Runs 1 and 2 suggests that the existence of the ambient magnetic field (in the Nitrogen plasma) is not a necessary condition for the formation of shocks in the Aluminum plasma.

In Run 3 where the magnetic field in the Aluminum plasma is absent, similar electron heating also takes place due to the penetration of the Aluminum ions (for $x > 0.637$ cm). The electron cyclotron drift instability is generated as in Run 1, and the spatial profile of the electron temperature is almost the same as that in Run 1. A strong fluctuation of the magnetic field is excited at $x \approx 0.637$ cm, and a part of Aluminum ions are reflected by the ponderomotive force. Since the gyration of Nitrogen ions is absent, the shock downstream is not formed in Run 3.

The Aluminum plasma pass through the Nitrogen plasma, and no interaction between them is seen in Run 4. The acceleration of Aluminum ions purely by the electrostatic field due to charge separation is seen in panel (b), which is weaker than the acceleration in the other runs. Also, electron heating due to the penetration of the Aluminum ions does not take place.

Finally, it should be noted that we also performed several runs with a large ambient magnetic field (e.g., 3 T and 5 T) in the Nitrogen plasma region. In these runs, a collisionless shock is formed by the gyration of Aluminum ions in the Nitrogen plasma region, which is consistent with the previous study. The influence of magnetic field in the Aluminum plasma due to the Biermann battery on the formation of discontinuities and shocks is small. Hence, these runs with a large ambient magnetic field are out of purpose of the present study and are not shown here.

IV. SUMMARY

The interaction between the piston Aluminum plasma and the ambient Nitrogen plasma was studied by means of a 1D full PIC simulations as a preliminary numerical experiment for laboratory experiment on the generation of magnetized collisionless shocks with high-power lasers. Preliminary numerical experiments are important in the prediction of results of laboratory experiments.

Four different runs were performed with the combination of two magnetized and/or unmagnetized plasmas. It is shown that the magnetic field plays an important role in the formation of the tangential EMHD discontinuity around the interface between the two plasmas in the present study with a weak ambient magnetic field. The tangential EMHD discontinuity is formed on the timescale of the electron gyro period. This result is different from the previous result in which a strong ambient magnetic field was imposed and shock waves were formed around the interface between the piston plasma and the background plasma.

A shock wave is formed through the gyration of the ambient plasma in the piston plasma region in the present study with a weak ambient magnetic field. The comparison among the four runs showed that a perpendicular collisionless shock is formed only when the piston plasma is magnetized. It is suggested that the spontaneous magnetic field in the piston plasma due to the Biermann battery plays an essential role in the formation of a perpendicular collisionless shock in the interaction between the two plasmas. The shock downstream is formed during the gyration of ambient ions in the piston plasma region on the timescale of quarter gyro period of ambient ions.

ACKNOWLEDGMENTS

This work was supported by JSPS KAKENHI grant numbers 18H01232(RY, TM), 16K17702 (YO), 15H02154, 17H06202 (YS), 17H18270 (SJT), and 17J03893 (TS). This work was also supported partially by the joint research project of the Institute of Laser Engineering, Osaka University. The computer simulations were performed on the CUDAS supercomputer system at the Institute for Space-Earth Environmental Research in Nagoya University under the joint research program.

Appendix A

Figure 5 shows the numerical dispersion relation of the electric field $E_x$ component in Run 1 obtained by Fourier transformation for $0.2 < x < 0.3$ cm and $3.9 < t < 4.68$ nsec with 12,050 points in position and 3000 points in time. The frequency and wavenumber are normalized by the angular cyclotron frequency $\omega_{ceb}$ and the inertial length $d_{eb}$ of the background electrons, respectively. The local electron cyclotron frequency $\omega_{ceb}$ is calculated from $\omega_{ceb} = \omega_{ce,local}$, where $\omega_{ce,local} \approx 35 \omega_{ceb}$ in both space and time due to the penetration of the Aluminum plasma. The spectral enhancement is seen in this frequency range. The plasma angular frequency of the background electrons is $\omega_{peb}/\omega_{ceb} \approx 78.74$, which is larger than the angular frequency of the excited waves. Hence, the waves are not excited at the local upper hybrid resonance frequency nor the local electron plasma frequency, but at the local electron cyclotron frequency. The phase velocity of the excited wave mode is obtained as $v_p \approx 1.5 \omega_{ceb}d_{eb} \approx 600$ km/s, which is close to the drift velocity of aluminum ions in this region as seen in Fig.1.


TABLE I. Simulation parameters for the present numerical experiment. A reduced value in the numerical experiment is shown at the right-hand side when the physical quantity is not the real one. The cyclotron frequency, the thermal gyro radius, the Alfvén velocity, and the plasma beta are for runs with non-zero magnetic field ($B_0 \neq 0$).

<table>
<thead>
<tr>
<th>Quantity</th>
<th>Aluminum plasma</th>
<th>Nitrogen plasma</th>
</tr>
</thead>
<tbody>
<tr>
<td>Drift velocity $V_d$ [km/s]</td>
<td>500</td>
<td>0</td>
</tr>
<tr>
<td>Magnetic field $B_0$ [T]</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Run 1</td>
<td>10.0</td>
<td>0.5</td>
</tr>
<tr>
<td>Run 2</td>
<td>10.0</td>
<td>0.0</td>
</tr>
<tr>
<td>Run 3</td>
<td>0</td>
<td>0.5</td>
</tr>
<tr>
<td>Run 4</td>
<td>0</td>
<td>0.0</td>
</tr>
<tr>
<td>Electrons</td>
<td>2,250/cell</td>
<td>90/cell</td>
</tr>
<tr>
<td>Density $N_e$ [cm$^{-3}$]</td>
<td>$3.75 \times 10^9$</td>
<td>$1.5 \times 10^{18}$</td>
</tr>
<tr>
<td>Plasma frequency $f_{pe}$ [Hz]</td>
<td>$5.51 \times 10^{13}$ / $5.51 \times 10^{12}$</td>
<td>$1.1 \times 10^{13}$ / $1.1 \times 10^{12}$</td>
</tr>
<tr>
<td>Temperature $T_e$ [eV]</td>
<td>10</td>
<td>30</td>
</tr>
<tr>
<td>Thermal velocity $V_{Te}$ [km/s]</td>
<td>1.330</td>
<td>2.300</td>
</tr>
<tr>
<td>Debye length $\lambda_{De}$ [m]</td>
<td>$3.71 \times 10^{-9}$ / $3.71 \times 10^{-8}$</td>
<td>$3.32 \times 10^{-8}$ / $3.32 \times 10^{-7}$</td>
</tr>
<tr>
<td>Inertial length $d_e$ [m]</td>
<td>$8.39 \times 10^{-7}$</td>
<td>$4.33 \times 10^{-6}$</td>
</tr>
<tr>
<td>Cyclotron frequency $f_{ce}$ [Hz]</td>
<td>$2.8 \times 10^{11}$</td>
<td>$1.4 \times 10^{10}$</td>
</tr>
<tr>
<td>Thermal gyro radius $r_e$ [m]</td>
<td>$7.55 \times 10^{-7}$</td>
<td>$2.62 \times 10^{-5}$</td>
</tr>
<tr>
<td>Plasma beta $\beta_e$</td>
<td>1.62</td>
<td>72.99</td>
</tr>
<tr>
<td>Ions</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Charge number $Z$</td>
<td>9</td>
<td>3</td>
</tr>
<tr>
<td>Mass ratio $m_i/m_e$</td>
<td>49572</td>
<td>25704</td>
</tr>
<tr>
<td>Density $N_i$ [cm$^{-3}$]</td>
<td>$4.17 \times 10^{18}$</td>
<td>$5.0 \times 10^{17}$</td>
</tr>
<tr>
<td>Plasma frequency $f_{pi}$ [Hz]</td>
<td>$7.43 \times 10^{11}$ / $7.43 \times 10^{10}$</td>
<td>$1.19 \times 10^{11}$ / $1.19 \times 10^{10}$</td>
</tr>
<tr>
<td>Temperature $T_i$ [eV]</td>
<td>10</td>
<td>30</td>
</tr>
<tr>
<td>Thermal velocity $V_{Ti}$ [km/s]</td>
<td>5.97</td>
<td>14.3</td>
</tr>
<tr>
<td>Debye length $\lambda_{Di}$ [m]</td>
<td>$3.71 \times 10^{-9}$ / $3.71 \times 10^{-8}$</td>
<td>$3.32 \times 10^{-8}$ / $3.32 \times 10^{-7}$</td>
</tr>
<tr>
<td>Inertial length $d_i$ [m]</td>
<td>$6.23 \times 10^{-5}$</td>
<td>$4.01 \times 10^{-4}$</td>
</tr>
<tr>
<td>Cyclotron frequency $f_{ci}$ [Hz]</td>
<td>$5.08 \times 10^{7}$</td>
<td>$1.63 \times 10^{6}$</td>
</tr>
<tr>
<td>Thermal gyro radius $r_i$ [m]</td>
<td>$1.87 \times 10^{-5}$</td>
<td>$1.4 \times 10^{-3}$</td>
</tr>
<tr>
<td>Alfvén velocity $V_A$ [km/s]</td>
<td>19.99</td>
<td>4.11</td>
</tr>
<tr>
<td>Plasma beta $\beta_i$</td>
<td>0.18</td>
<td>24.33</td>
</tr>
<tr>
<td>Grid spacing $\Delta x$ [m]</td>
<td>$8.3 \times 10^{-8}$</td>
<td></td>
</tr>
<tr>
<td>Time step $\Delta t$ [sec]</td>
<td>$2.6 \times 10^{-15}$</td>
<td></td>
</tr>
<tr>
<td>Number of grids $N_x$</td>
<td>120,000</td>
<td></td>
</tr>
<tr>
<td>Number of steps $N_t$</td>
<td>6,000,000</td>
<td></td>
</tr>
<tr>
<td>Speed of light $c$ [km/s]</td>
<td>$300,000$ / $30,000$</td>
<td>(laboratory) / (numerical)</td>
</tr>
</tbody>
</table>
FIG. 1. Temporal development of the interaction between the Aluminum plasma and the Nitrogen plasma for Run 1. The $x - v_x$ phase-space plots of ions at different times together with the spatial profile of the electron density.
FIG. 2. (a) Ion $x - v_x$ phase space together with the spatial profile of the electron density around the interface between the Aluminum plasma and the Nitrogen plasma at $t = 4.004$ nsec for Run 1. (b) Electron $x - v_x$ phase space together with the spatial profile of the electron temperature of the Aluminum (piston) plasma. (c) Electron $x - v_x$ phase space together with the spatial profile of the electron temperature of the Nitrogen (background) plasma. (d) Spatial profiles of the pressures of the piston electrons $P_{ep}$, the background electrons $P_{eb}$, the Aluminum ions $P_{Al}$, and the magnetic pressure $P_B$. The pressure is normalized to the initial electron pressure in the Nitrogen (background) plasma region.
FIG. 3. (a) Ion $x - v_x$ phase space together with the ion temperature of the Aluminum plasma around the gyrating Nitrogen ions at $t = 12.012$ nsec for Run 1, and (b) the corresponding ion $x - v_x$ phase space together with the spatial profile of the ion temperature for the Nitrogen plasma. (c) Electron $x - v_x$ phase space together with the spatial profile of the electron temperature. (d) Spatial profiles of the electron bulk velocity $U_{xe}$ and the magnetic field $B_y$. 
FIG. 4. Snapshot of four Runs at $t = 14.040$ nsec. (a) The $x - v_x$ phase-space plots of electrons. (b) The $x - v_x$ phase-space plots of ions. (c) The spatial profile of the magnetic field $B_y$ component. (d) The spatial profile of the electron density $N_e$. (e) The spatial profile of the electron temperature $T_e$. 
FIG. 5. Numerical dispersion relation of the electric field $E_x$ component in Run 1 obtained by Fourier transformation for $0.2 < x < 0.3$ cm and $3.9 < t < 4.68$ nsec. The frequency and wavenumber are normalized by the angular cyclotron frequency $\omega_{ceb}$ and the inertial length $d_{eb}$ of the background electrons, respectively.